

Lecture 6

Top-Down Parsing :-

Top-down parsing can be viewed as an attempt to find a *leftmost derivation* for an input string. Equivalently, A top down parser, such as LL(1) parsing, move from the goal symbol to a string of terminal symbols. in the terminology of trees, this is moving from the root of the tree to a set of the leaves in the syntax tree for a program. in using full backup we are willing to attempt to create a syntax tree by following branches until the correct set of terminals is reached. in the worst possible case, that of trying to parse a string which is not in the language, all possible combinations are attempted before the failure to parse is recognized. the nature of top down parsing technique is characterized by:

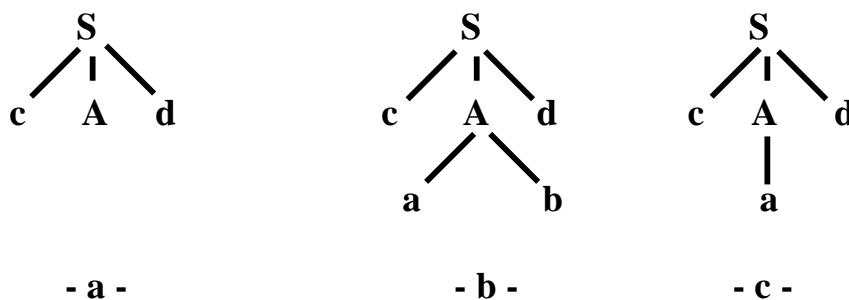
1-Recursive-Descent Parsing : It is a general form of Top-Down Parsing that may involve " *Backtracking* ",that is ,making repeated scans of the input.

Example: consider the grammar

$$\begin{aligned} S &\longrightarrow cAd \\ A &\longrightarrow ab \mid a \end{aligned}$$

Input : **cad**

Then the implementation of Recursive-Descent Parsing is:



2-Predictive parsing : In many cases, by carefully writing a grammar , eliminating *left-recursion* from it and *left-factoring* the resulting grammar, we can obtain a grammar that can be parsed by *recursive-descent parser* that needs no "*Backtracking*",i.e.,a **Predictive parser**.

2.1. Transition Diagrams for Predictive parsers

It is useful plan or flowchart for a predictive parser. There is one diagram for each *nonterminal*, the labels of edges are *tokens* and *nonterminals*.for example:

$$E \rightarrow E+T \mid T$$

$$T \rightarrow T*F \mid F \quad // \text{ Original grammar}$$

$$F \rightarrow (E) \mid id$$

Eliminate left-recursion and left factoring

$$E \rightarrow T E'$$

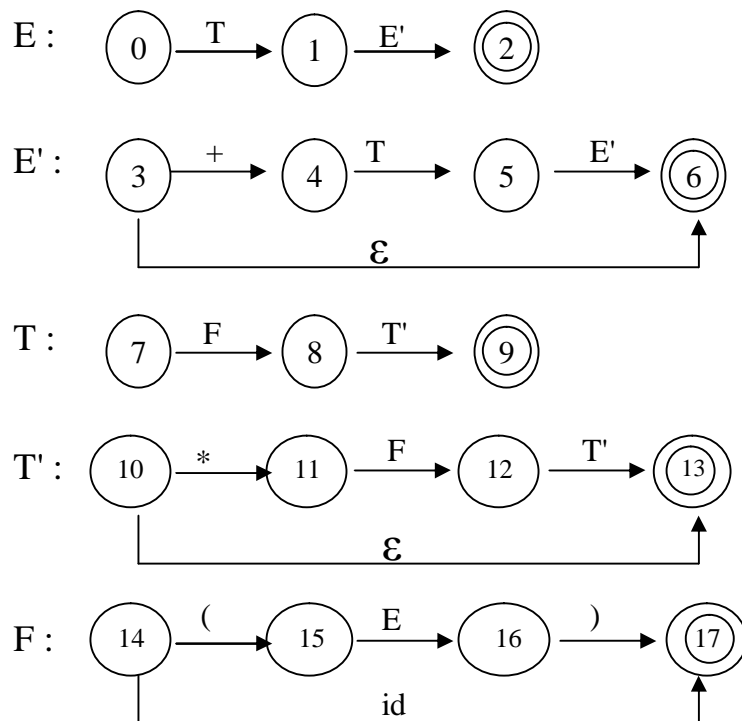
$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

Transition Diagrams



First & Follow :

- **First :** To compute First(X) for all grammar symbols apply the following rules until no more *terminal* or ϵ can be added to any First set :
 1. If x is *terminal*, then **FIRST(x)** is {x}.
 2. If $x \rightarrow \epsilon$ is a production ,then add ϵ to FIRST(x).
 3. If x is *nonterminal* and $x \rightarrow y_1 y_2 \dots y_k$ is a production, then place a in FIRST(x) if for some i , a is in FIRST(y_i),and ϵ is in all of FIRST(y_1)... FIRST(y_{i-1}).
- **Follow :** To compute Follow(A) for all *nonterminals* apply the following rules until nothing can be added to any Follow set.
 1. Place \$ in FOLLOW(S),where S is the start symbol.
 2. If there are a production $A \rightarrow \alpha B \beta$, then everything in FIRST(β)except for ϵ is placed in FOLLOW(B).
 3. If there are a production $A \rightarrow \alpha B$,or a production $A \rightarrow \alpha B \beta$ where FIRST(β) contains ϵ , then everything in FOLLOW(A) is in FOLLOW(B).

Example : suppose the following grammar

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' \mid \epsilon$$

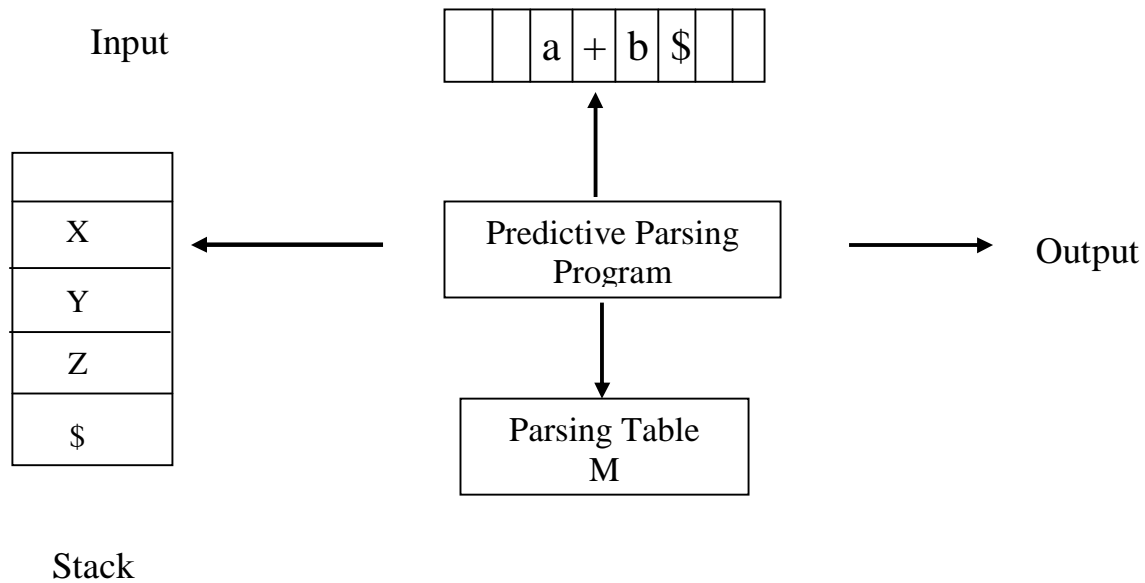
$$T \rightarrow F T'$$

$$T' \rightarrow * F T' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

Nonterminals	First	Follow
E	(, id) , \$
E'	+ , ϵ) , \$
T	(, id	+ ,) , \$
T'	* , ϵ	+ ,) , \$
F	(, id	* , + ,) , \$

2.2. Nonrecursive Predictive Parsing :-The nonrecursive parser in following figure lookup the production to be applied in a parsing table.



Model of a Nonrecursive Predictive Parsing

- **Construction of Predictive Parsing Table :**

1. For each production $A \rightarrow \alpha$ of the grammar, do steps 2 and 3 .
2. For each terminal a in $\text{First}(\alpha)$, add $A \rightarrow \alpha$ to $M[A, a]$.
3. If ϵ is in $\text{First}(\alpha)$,add $A \rightarrow \alpha$ to $M[A, b]$ for each b in $\text{Follow}(A)$.
4. Make each undefined entry of M be error.

- **Predictive Parsing Program :**The parser is controlled by a program that behaves as follows:
The program consider X- the symbol on top of the stack- and a – the current input symbol-. These two symbols determine the action of the parser. There are three possibilities :

1. If $X = a = \$$, the parser halt, and successful completion of parsing.
2. If $X = a \neq \$$, the parser pops X off the stack and advances the input pointer to the next input symbol.
3. If X is nonterminal , the program consults entry $M[X,a]$ of the parsing table.If $M[X,a]=\{ X \rightarrow UVW \}$ the parser replaces X on top of stack by WVU (with U on top).

Example:

$$E \rightarrow E+T \mid T$$

$$T \rightarrow T * F \mid F \quad // \text{ Original grammar}$$

$$F \rightarrow (E) \mid \text{id}$$

Eliminate left-recursion and left factoring

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \text{id}$$

Predictive Parsing Table M

Nonterminals	Input symbol					
	id	+	*	()	\$
E	TE'			TE'		
E'		+TE'			ϵ	ϵ
T	FT'			FT'		
T'		ϵ	*FT'		ϵ	ϵ
F	id			(E)		

Implement Predictive Parsing Program

stack	Input	output
\$E	id+id*id\$	
\$E'T	id+id*id\$	$E \rightarrow TE'$
\$E'T'F	id+id*id\$	$T \rightarrow FT'$
\$E'T'id	id+id*id\$	$F \rightarrow id$
\$E'T'	+id*id\$	
\$E'	+id*id\$	$T' \rightarrow \epsilon$
\$E'T+	+id*id\$	$E' \rightarrow +TE'$
\$E'T	id*id\$	
\$E'T'F	id*id\$	$T \rightarrow FT'$
\$E'T'id	id*id\$	$F \rightarrow id$
\$E'T'	*id\$	
\$E'T'F*	*id\$	$T' \rightarrow *FT'$
\$E'T'F	id\$	
\$E'T'id	id\$	$F \rightarrow id$
\$E'T'	\$	$T' \rightarrow \epsilon$
\$E'	\$	$E' \rightarrow \epsilon$
\$	\$	Accept

LL(1)Grammar :A grammar whose parsing table has no multiply-defined entries is said to be LL(1).

Example :- (H.W)

$S \rightarrow iEtSS' \mid a$

$S' \rightarrow eS \mid \epsilon$

$E \rightarrow b$

Everything Comes to him who Waits